

D.O.E.-05/08/2026

MM-

30(10×3)

TIME-1 HOUR

(1) A circular wire of radius 7.5 cm is cut and bent so as to lie along the circumference of a hoop whose radius is 120 cm. Find in degrees the angle which is subtended at the centre of the hoop.

(2) Prove that

$$\tan\left(\frac{11\pi}{3}\right) - 2 \sin\left(\frac{4\pi}{3}\right) - \frac{3}{4} \operatorname{cosec}^2\left(\frac{\pi}{4}\right) + 4 \cos^2\left(\frac{17\pi}{6}\right) = \frac{3 - 4\sqrt{3}}{2}$$

(3) If $\theta = \frac{\pi}{2^n + 1}$, prove that $2^n \cos \theta \cos 2\theta \cos 2^2\theta \dots \cos 2^{n-1}\theta = 1$

(4) Prove that $\cos 5A = 16 \cos^5 A - 20 \cos^3 A + 5 \cos A$

(5) Derive the value of $\sin 72^\circ$.

(6) Prove that $\frac{\sec 8\theta - 1}{\sec 4\theta - 1} = \frac{\tan 8\theta}{\tan 2\theta}$

(7) If $\sin \theta = n \sin(\theta + 2\alpha)$, prove that $\tan(\theta + \alpha) = \frac{1 + n}{1 - n} \tan \alpha$

(8) Prove that $\sin 10^\circ \sin 30^\circ \sin 50^\circ \sin 70^\circ = \frac{1}{16}$

(9) If $\tan A - \tan B = x$ and $\cot B - \cot A = y$, prove that $\cot(A - B) = \frac{1}{x} + \frac{1}{y}$

(10) If $\tan 35^\circ = a$, Prove that $\frac{\tan 145^\circ - \tan 125^\circ}{1 + \tan 145^\circ \tan 125^\circ} = \frac{1 - a^2}{2a}$